

# Statistics

## Lecture 10



Feb 19-8:47 AM

A piggy bank has 5 Dimes, 8 nickels, and 7 quarters. If we randomly select one coin

$$1) P(\text{Dime}) = \frac{5}{20} = \frac{1}{4} = .25$$

20 Coins  
total

$$2) P(\text{Nickel}) = \frac{8}{20} = \frac{2}{5} = .4$$

$$3) P(\overline{\text{Quarter}}) = 1 - P(\text{Quarter}) = 1 - \frac{7}{20} = \frac{13}{20} = .65$$

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Suppose  $P(A) = .025$

1) Find  $P(A)$  in reduced fraction.

$$.025 \quad \boxed{\text{MATH}} \quad \boxed{1: \triangleright \text{Frac}} \quad \boxed{\text{Enter}} \quad \frac{1}{40}$$

2) Write  $P(A)$  in % Notation.

$$.025 = \underbrace{.025(100)}\% = \boxed{2.5\%}$$

3) Find  $P(\bar{A}) = 1 - P(A) = 1 - .025 = \boxed{.975}$

4) Simplify  $\frac{P(\bar{A})}{P(A)} = \frac{.975}{.025} = \boxed{39}$

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Are you in support of mass deportation?

|             | Yes | NO  | Total |
|-------------|-----|-----|-------|
| Republicans | 120 | 30  | 150   |
| Democrats   | 100 | 250 | 350   |
| Indep.      | 50  | 50  | 100   |
| Total       | 270 | 330 | 600   |

If we randomly select one of them,

$$1) P(\text{Democrat}) = \frac{350}{600} = \frac{7}{12} \quad 2) P(\text{NO}) = \frac{330}{600} = \frac{11}{20}$$

$$3) P(\text{Democrat and NO}) = \frac{250}{600} = \frac{5}{12}$$

$$4) P(\text{Democrat or No}) = \frac{430}{600} = \frac{43}{60}$$

$$5) P(\text{Republican and Independent}) = \frac{0}{600} = \boxed{0}$$

Do not use  $\emptyset$  for 0.

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Suppose  $P(A) = .35$  ,  $P(B) = .75$  ,  $P(A \text{ and } B) = .15$

1)  $P(\bar{A}) = 1 - P(A) = .65$

2)  $P(\bar{B}) = 1 - P(B) = .25$

3)  $P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .15 = .85$

4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 Addition Rule  $= .35 + .75 - .15 = .95$

5) Construct Venn Diagram

$P(A \text{ only}) = .35 - .15 = .2$

$P(B \text{ only}) = .75 - .15 = .6$

6)  $P(A \text{ only or } B \text{ only}) = .2 + .6 = .8$

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Suppose  $P(A) = .3$  ,  $P(B) = .6$  ,  $A$  and  $B$  are Mutually Exclusive Events

1)  $P(\bar{A}) = .7$

2)  $P(\bar{B}) = .4$

3)  $P(A \text{ and } B) = 0$

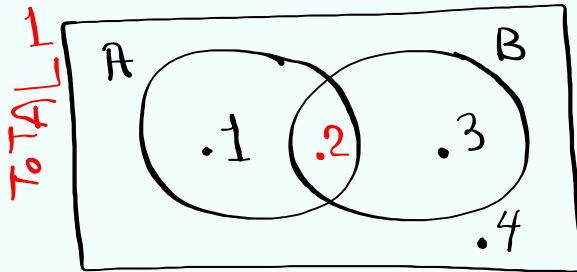
4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $= .3 + .6 - 0 = .9$

5) Construct Venn Diagram

Total = 1 ✓

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Complete the Venn diagram below



1)  $P(A) = .3$

2)  $P(A \text{ only}) = .1$

3)  $P(B) = .5$

4)  $P(B \text{ only}) = .3$

5)  $P(A \text{ or } B) = .3 + .5 - .2 = \boxed{.6}$

$\hookrightarrow .1 + .2 + .3 = \boxed{.6}$

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De Morgan's Law

$P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B})$

$P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B})$

Suppose  $P(A) = .45$ ,  $P(B) = .65$ ,  $P(A \text{ or } B) = .9$

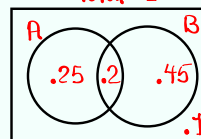
1)  $P(\bar{A}) = \boxed{.55}$

2)  $P(\bar{B}) = \boxed{.35}$

3)  $P(A \text{ and } B)$

4) Draw Venn Diagram. Total = 1

$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $\boxed{.9} = .45 + .65 - P(A \text{ and } B)$



$P(A \text{ and } B) = .45 + .65 - .9 = \boxed{.2}$

5)  $P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .9 = \boxed{.1}$

De Morgan's Law

6)  $P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .2 = \boxed{.8}$

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## odds vs Probability

odds in favor of event  $E$  are

$$a : b$$

odds against event  $E$  are  $b : a$ 

I flipped a coin 100 times.

It landed tails 60 times.

$$P(\text{Tails}) = \frac{60}{100} = \boxed{.6}$$

odds in favor of landing tails are

$$60 \text{ tails} : 40 \text{ tails}$$

$$60 : 40 \rightarrow \boxed{3 : 2}$$

$$\begin{array}{l} \text{odds against} \\ \text{landing tails} \end{array} \rightarrow 2 : 3$$

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Standard deck of playing cards

52 Cards      4 Aces

$$P(\text{Draw an Ace}) = \frac{4}{52} = \boxed{\frac{1}{13}}$$

odds in favor of drawing an ace

$$\# \text{ Aces} : \# \overline{\text{Aces}}$$

$$4 : 48 \Rightarrow \boxed{1 : 12}$$

$$4 \div 48 \quad \boxed{\text{Math}} \quad \boxed{1 : \rightarrow \text{frac}} \quad \boxed{\text{Enter}} \quad \frac{1}{12}$$

Odds against drawing an ACE

$$\boxed{12 : 1}$$

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Suppose odds for Lakers to win the championship this Year are 1:7

1) odds against 7:1

2) Meaning of 1:7

\$1 → \$7 Net profit

+250 → \$100 bet → \$250 Net

-150 → \$150 → \$100

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How to find odd if  $P(E)$  is given.  
 odds in favor of event  $E$  are  
 $P(E) : P(\bar{E})$   
 Always simplify

ex: Suppose  $P(E) = .025$

1)  $P(\bar{E}) = .975$

2) odds in favor of event  $E$

$P(E) : P(\bar{E})$   
 $.025 : .975$

$1 : 39$

$.025 \div .975$  [MATH] [1:] [frac] [Enter]  $\frac{1}{39}$

odds against 39:1

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$P(\text{Lakers win championship this year}) = .24$

$$P(W) = .24$$

$$P(\bar{W}) = .76$$

odds in favor of  $W$

$$P(W) : P(\bar{W})$$

$$.24 : .76 \rightarrow \boxed{6 : 19}$$

Place \$6 bet

odds against

$$19 : 6$$

If they win, you get \$19  
Profit

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How to find  $P(E)$  if odds <sup>in favor</sup> are given  
 $a : b$

$$P(E) = \frac{a}{a+b}$$

$$P(\bar{E}) = \frac{b}{a+b}$$

ex: Suppose odds in favor of event  
 $E$  are  $4 : 21$ .

$$1) P(E) = \frac{4}{4+21} = \boxed{\frac{4}{25}}$$

$$2) P(\bar{E}) = \frac{21}{4+21} = \boxed{\frac{21}{25}}$$

3) odds against  $E$ .  $\boxed{21 : 4}$

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Multiplication Rule

Key word AND

Event requires more than one action

Consider a deck of playing cards,  
Draw  $\geq$  Cards

R  $\rightarrow$  Red                      RR    RB    BR    BB  
B  $\rightarrow$  Black

A Family with 3 kids

B  $\rightarrow$  Boy  
G  $\rightarrow$  Girl

Sample Space

BBB  
BBG  
BGB  
BGG  
GBB  
GBG  
GGB  
GGG

Complete list of all possible outcomes

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Independent events

when one outcome does not change the prob. of next outcome.

Draw  $\geq$  Cards

$P(\text{both are aces}) = P(\text{Ace}) \cdot P(\text{Ace})$

with replacement

$$= \frac{4}{52} \cdot \frac{4}{52} = \frac{1}{13} \cdot \frac{1}{13} = \boxed{\frac{1}{169}}$$

$P(A \text{ and } B) = P(A) \cdot P(B)$

when A & B are independent events

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You are taking a quiz with two questions.

Each question is multiple-choice.

4 choices one correct choice

You make random guesses.

$$P(\text{both correct}) = P(\text{correct}) \cdot P(\text{correct})$$

$$= \frac{1}{4} \cdot \frac{1}{4} = \frac{1}{16}$$

$$P(\text{both incorrect}) = P(\overline{\text{correct}}) \cdot P(\overline{\text{correct}})$$

$$= \frac{3}{4} \cdot \frac{3}{4} = \frac{9}{16}$$

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Tree Diagram  
 Draw 2 Cards  
 with replacement

A → Ace  
 $\bar{A}$  →  $\bar{\text{Ace}}$

First Draw

AA      A $\bar{A}$        $\bar{A}A$        $\bar{A}\bar{A}$

$$P(\bar{A}\bar{A}) = \frac{48}{52} \cdot \frac{48}{52} = \frac{144}{169}$$

48 ÷ 52 × 48 ÷ 52 MATH 1: ▸ frac Enter

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